A negative imaginary solution to an aircraft platooning problem

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Abstract—Over the next decade, the growth of commercial aircraft is expected to increase by 30%, causing significant challenges in air traffic management and control. To address this problem, we propose the idea of aircraft platooning during the descending and pre-landing phases. The objective is to design a distributed flight guidance and control system that assists onboard pilots in finding a feasible and collision-free trajectory from descent to pre-landing. The proposed aircraft platoon control scheme comprises a feedback linearising controller in the inner loop that transforms the nonlinear aircraft dynamics into a MIMO double-integrator, inherently a Negative Imaginary system. The outer loop employs a distributed output feedback Strictly Negative Imaginary controller, enabling networked aeroplanes to maintain the desired inter-aircraft spacing along each coordinate by synchronising their velocities. In addition, a contingency strategy is proposed to handle potential runway failures (e.g., sudden blockage, damage, etc.) by switching a descending aircraft platoon into a time-varying hover formation for each aircraft, maintaining a safe vertical gap. Finally, a comprehensive MATLAB simulation case study is conducted to test the feasibility and performance of the NI theory-based aircraft platoon control scheme.

I. INTRODUCTION

Due to the consistent growth in the civil aviation sector over the last three decades, the number of commercial aircraft has continuously increased [1], consequently leading to a sharp rise in the number of incoming flights (i.e., those approaching for landing) at each airport. This trend is particularly concerning and significant for busy airports such as Atlanta, Dubai, Tokyo, London Heathrow, Dallas, Los Angeles, Paris, Frankfurt, Istanbul, etc. Despite the dedicated efforts of Air Traffic Control (ATC) at every airport, there remains a risk of failure if the number of incoming air traffic exceeds the maximum capacity of an airport or in emergencies. One possible solution is expanding the capacity of an airport. However, this might not always be feasible due to geographical, socio-economic, and safety constraints [2]. Another approach involves optimising the aircraft scheduling problem [3] through improved communication systems, advanced routing algorithms, and fail-safe ATC software.

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Fig. 1. (a) A descending aircraft platoon proceeding for a regular (or uninterrupted) landing; (b) The descending aircraft platoon switches to a hovering state to wait when the landing runway is not ready.

A potential alternative is introducing the idea of aircraft platooning, as illustrated in Fig. 1. This new concept demonstrates how a fleet of descending aircraft aiming to land at a particular airport can form a platoon and synchronise their motions to maintain the desired inter-aircraft spacing throughout the descending and pre-landing phases. Aircraft platooning significantly helps reduce air traffic congestion, improve operational efficiency, and enhance safety. In addition, it greatly reduces dependence on a centralised and human-operated air traffic control system while optimising runway usage.

The idea of aircraft platooning has been inspired by the concept of vehicle platooning (see [4] and the references therein), which ensures a desired inter-vehicular spacing by synchronising the velocities of all the vehicles in a fleet [5]. Major applications of vehicle platooning include the cruise control of automated vehicles (such as cars, buses, trucks) [6], control of connected train platoons [7], energy-saving aircraft formation flight [8]. With the advancements of graph theory-based cooperative control of multi-agent
systems (MASs) [9], [10], the literature on vehicle platooning has been substantially enriched. Lately, the Negative Imaginary (NI) systems theory has also emerged as a vital technique for multi-agent vehicle platooning since its introduction in 2007-2008 [11]. This property is commonly observed in flexible structures and Euler-Lagrange systems with collocated position sensors and force actuators [11], [12]. Over the last few years, the NI systems theory has found promising applications in the cooperative control of various MASs, starting with [13], particularly in multi-UGV systems [14], multi-UAV systems [15]–[18], and train platoons [7].

Driven by a strong urge to find a feasible, reliable and fail-safe solution to the continuously increasing air traffic problem, especially at busy airports, we bring the idea of fail-safe solution to the multi-agent vehicle platooning with collocated position sensors and force actuators [11], [19]–[21].

This paper introduces the idea of aircraft platooning to facilitate a smooth, hassle-free, minimum-delay and fail-safe landing, especially at busy airports. It ensures the descending aircraft agents maintain the desired inter-aircraft spacing in all coordinates; An NI theory-based two-loop control scheme is proposed to achieve the desired aircraft platooning objectives. The inner loop applies a feedback-linearising control action to transform the nonlinear translational double-integrator system. While the outer loop implements a distributed output feedback SNI controller;

To tackle the runway unavailability issues due to blockage or disruptions, a contingency strategy is devised that helps a descending aircraft platoon switch to a hover formation at different altitudes, maintaining a constant vertical gap while waiting for a landing runway;

The proposed control scheme is completely distributed and requires only the output feedback (i.e., the position information) of the neighbouring aircraft agents, as illustrated in Fig. 1 and Fig. 2b.

The notations and acronyms adhere to standard conventions. The set of real numbers is denoted by \( \mathbb{R} \). The 2-norm of a vector is denoted by \( \| \cdot \| \). A \( A > 0 \) denotes that a matrix \( A \) is positive definite. The complex conjugate transpose of a matrix \( A \) is denoted by \( A^* \). The Kronecker product of two matrices, \( A \) and \( B \), is represented by \( A \otimes B \). \( \mathbb{S}^{m \times n} \) denotes the space of all real, rational, proper transfer function matrices of dimension \( (m \times n) \).

II. TECHNICAL BACKGROUND

A. Definitions of NI and SNI systems

This subsection revisits the definitions of NI and SNI systems.

**Definition 1: (NI Systems) [19]** A system \( T(s) \in \mathbb{R}^{m \times m} \) is said to be an NI system if: (i) it has no right-half plane poles; (ii) \( j[T(j\omega) - T(j\omega)^*] \geq 0 \ \forall \omega \in (0, \infty) \) except the values of \( \omega \) where \( s = j\omega \) is a pole of \( T(s) \); (iii) \( s = j\omega_0 \) with \( \omega_0 \in (0, \infty) \) is a pole of \( T(s) \), then it is at most a simple pole and \( \lim_{s \to j\omega_0} (s - j\omega_0)T(s) \geq 0 \); and (iv) \( s = 0 \) is a pole of \( T(s) \), then \( \lim_{s \to 0} s^kT(s) \geq 0 \ \forall k \geq 3 \) and \( \lim_{s \to 0} s^2T(s) \geq 0 \).

**Definition 2: (SNI Systems) [11], [19]** A system \( T(s) \in \mathbb{R}^{m \times m} \) is said to be an SNI system if \( j[T(j\omega) - T(j\omega)^*] > 0 \ \forall \omega \in (0, \infty) \).

B. Interaction topology

We describe the interaction topology among networked aircraft agents using a weighted and undirected graph \( G = (\mathcal{V}, \mathcal{E}) \), where \( \mathcal{V} = \{1, \ldots, N\} \) is the node-set, \( \mathcal{E} \subset \mathcal{E} \times \mathcal{E} \) is the edge set, and \( \mathcal{E} = [a_{ij}] \in \mathbb{R}^{N \times N} \) is the adjacency matrix. The edge \( e_{ji} = (v_j, v_i) \in \mathcal{E} \) denotes the information flow from node \( j \) to node \( i \). We denote the neighbour set of node \( i \) as \( \mathcal{N}_i = \{v_j | (v_j, v_i) \in \mathcal{E}\} \), \( a_{ij} \) represents the weight of \( e_{ji} \), with \( a_{ij} > 0 \) if \( e_{ji} \in \mathcal{E} \). The indegree matrix is denoted by \( \mathcal{D} = \text{diag}(d_1, d_2, \ldots, d_N) \) with \( d_i = \sum_{j=1}^{N} a_{ij} \ \forall i \in \{1, \ldots, N\} \). The Laplacian matrix \( \mathcal{L} \in \mathbb{R}^{N \times N} \) is given by \( \mathcal{L} = \mathcal{D} - \mathcal{A} \). If the \( i \)-th aircraft is connected to the virtual leader agent (denoted as ‘0’) via a directional link, an edge \( e_0i \), exists between them, characterised by a positive pinning gain \( g_i > 0 \). The pinning-gain matrix is denoted by \( \mathcal{G} = \text{diag}(g_1, g_2, \ldots, g_N) > 0 \).

**Assumption 1:** The interaction topology of \( N \) networked aircraft agents is described by an undirected and connected graph \( G \). We assume there is a root node (known as the ‘virtual leader’) that provides a reference trajectory (i.e. \( r_0 \in \mathbb{R}^3 \)) to the aircraft platoon (at least to one aircraft agent). Due to Assumption 1, in the case of an undirected graph \( G \), we can derive that \( (\mathcal{L} + \mathcal{G}) > 0 \).

C. Properties of multi-agent NI and SNI systems

This paper employs multi-agent NI theory to model and control an aircraft platoon whose nonlinear dynamics can be feedback-linearised into a decoupled three-input-three-output double-integrator system that automatically exhibits the NI systems properties. This subsection will revisit some useful properties of multi-agent NI systems.

**Lemma 1:** [20], [21]. Let a homogeneous networked stable NI (or SNI) system be comprised of \( N \) agents \( T(s) \) that satisfies Assumption 1. Then, \( \bar{T}(s) = (\mathcal{L} + \mathcal{G}) \otimes T(s) \) is stable NI (or SNI) if and only if \( T(s) \) is NI (or SNI).

**Theorem 1:** [15] Consider a double-integrator MAS, \( I_N \otimes T(s) \), coupled with an undirected graph \( G \) satisfying Assumption 1. Let this MAS be interconnected with a distributed SNI controller, \( I_N \otimes \beta T_r(s) \), via positive feedback, as shown in Fig. 2a. Then, the closed-loop system is asymptotically stable for any \( \beta \in (0, \infty) \) if \( T_r(0) < 0 \).

III. MODELLING AND PROBLEM FORMULATION

This section derives the feedback-linearised aircraft model and formulates the aircraft platooning problem.

A. Dynamic model of an aircraft

We consider a point-mass aircraft model [22], [23] to describe the motion of each aircraft in the networked aircraft. The point-mass aircraft model is given by:

\[
\dot{x} = v \\
\dot{v} = -\frac{1}{m} \left[ \sum_{j=1}^{N} a_{ij} \left( v_j - v_i \right) + \mathcal{G} v_i + \mathcal{L} (r_0 - r_i) \right]
\]
platoon. The kinematic equations of the $i$th aircraft can be represented by

$$\begin{align*}
\dot{x}_i &= V_i \cos \gamma_i \cos \chi_i, \\
\dot{y}_i &= V_i \cos \gamma_i \sin \chi_i, \\
\dot{h}_i &= V_i \sin \gamma_i,
\end{align*}$$

where $x_i$ is the downrange, $y_i$ is the cross-range, $h_i$ is the altitude, $V_i$ is the airspeed, $\gamma_i$ is the flight-path angle and $\chi_i$ is the heading angle. The equations governing the dynamics of the $i$th aircraft are given by

$$\begin{align*}
\dot{V}_i &= \frac{T_i - D_i}{m_i} - g \sin \gamma_i, \\
\dot{\gamma}_i &= \frac{g}{V_i} (n_i \cos \phi_i - \cos \gamma_i), \\
\dot{\chi}_i &= \frac{g n_i \sin \phi_i}{V_i \cos \gamma_i},
\end{align*}$$

where $T_i$ represents the engine thrust, $D_i$ denotes the aerodynamic drag, $m_i$ is the mass of the aircraft, and $g$ is the acceleration due to gravity. In this model, the control variables are the engine thrust $T_i$ controlled by the throttle, the g-load $n_i$ regulated by the elevator, and the banking angle $\phi_i$ manipulated through the rudder and ailerons.

The above nonlinear aircraft model in (1) and (2) can be effectively transformed into a decoupled three-input-three-output double-integrator system via feedback linearisation [22], [23]. By differentiating the kinematics in (1) w.r.t. time and substituting with the dynamics in (2), one obtains

$$\begin{align*}
\ddot{x}_i &= u_{x_i} = \frac{T_i - D_i}{m_i} c_{\chi_i} c_{\gamma_i} - g n_i (s_{\gamma_i} c_{\chi_i} c_{\phi_i} + s_{\chi_i} s_{\phi_i}), \\
\ddot{y}_i &= u_{y_i} = \frac{T_i - D_i}{m_i} c_{\gamma_i} s_{\chi_i} - g n_i (s_{\gamma_i} s_{\chi_i} c_{\phi_i} - c_{\chi_i} s_{\phi_i}), \\
\ddot{h}_i &= u_{h_i} = \frac{T_i - D_i}{m_i} s_{\gamma_i} + g n_i c_{\gamma_i} c_{\phi_i} - g,
\end{align*}$$

where $u_{x_i}$, $u_{y_i}$, and $u_{h_i}$ are the new control variables (i.e. the acceleration components of the $i$th aircraft in each coordinate) in the linearised double-integrator model. Note that $c_{\phi} \triangleq \cos \phi$ and $s_{\phi} \triangleq \sin \phi$. The relation between the new control variables and the actual control variables can be expressed as follows:

$$\begin{align*}
\phi_i &= \tan^{-1} \left( \frac{u_{x_i} c_{\chi_i} - u_{x_i} s_{\chi_i} s_{\phi_i}}{c_{\gamma_i} (u_{h_i} + g) - s_{\gamma_i} (u_{x_i} c_{\gamma_i} + u_{y_i} s_{\chi_i})} \right), \\
n_i &= c_{\gamma_i} (u_{h_i} + g) - s_{\gamma_i} (u_{x_i} c_{\gamma_i} + u_{y_i} s_{\chi_i}), \\
T_i &= [s_{\gamma_i} (u_{h_i} + g) + c_{\gamma_i} (u_{x_i} c_{\chi_i} + u_{y_i} s_{\chi_i})] m_i + D_i.
\end{align*}$$

B. Problem statement

Consider $N$ aircraft agents whose nonlinear dynamics model can be feedback-linearised into a decoupled three-input-three-output double-integrator system: $p_i = v_i, \quad \dot{v}_i = u_i$, where $p_i = [x_i, y_i, h_i]^T$ is the position vector, $v_i = [v_{x_i}, v_{y_i}, v_{h_i}]^T$ is the velocity vector and $u_i = [u_{x_i}, u_{y_i}, u_{h_i}]$ is the control input vectors of the $i$th aircraft. The aim is to develop a distributed flight guidance and control system to address the challenge of aircraft platooning, as illustrated in Fig. 1. The control objectives are as follows:

1) During regular aircraft landings, as described in Fig. 1a, each aircraft in the platoon should maintain the desired inter-aircraft spacing with successive aircraft along each coordinate. Furthermore, all aircraft should converge towards a constant velocity, synchronising with the speed of the virtual leader agent. That is

$$\begin{align*}
\lim_{t \to \infty} p_i(t) - p_j(t) &= d_i - d_j, \\
\lim_{t \to \infty} v_i(t) - v_0(t) &= 0,
\end{align*}$$

for all $i, j \in \{1, 2, \ldots, N\}$ and $i \neq j$, where $v_0(t)$ is the velocity of the virtual leader agent. The desired inter-aircraft spacing is defined as $d_i = [x_i, y_i, h_i]^T$ and $d_j$ represent the projected distances along the $X, Y,$ and altitude coordinates, respectively.

2) When a runway fault occurs during aircraft landings, as described in Fig. 1b, each aircraft should transition to a time-varying hover formation at a different altitude while maintaining a constant vertical gap. That is

$$\lim_{t \to \infty} p_i(t) - p_j(t) = d_i(t) - d_j(t),$$

where the time-varying hover formation is defined as $d_i(t) = [x_i, y_i, h_i(t)]^T$ and $d_j$ represent the projected distances along the $X, Y,$ and altitude coordinates, respectively.
\{1, 2, \ldots, N\}. Here, \(f_x(t)\) and \(f_y(t)\) are the pre-specified time-varying hover formation configurations.

IV. AN NI THEORY-BASED AIRCRAFT PLATOON CONTROL SCHEME

This section establishes the theoretical foundation for the proposed two-loop aircraft platoon control scheme, as shown in Fig. 2b, relying on the NI systems theory. The idea stems from the observation that a nonlinear aircraft model can be feedback-linearised into a decoupled three-input-three-output double-integrator system that inherently exhibits the NI property. Drawing insights from recent advancements in NI-based cooperative control techniques, we propose a novel distributed SNI output feedback cooperative controller to achieve the stated aircraft platooning objectives.

**Theorem 2:** Consider a platoon of \(N\) aircraft agents whose nonlinear translational dynamics can be feedback-linearised into a three-input-three-output double-integrator system \(I_3 \otimes T(s)\), where \(T(s) = \frac{1}{s^2}\). Suppose the interaction topology satisfies Assumption 1. Choose a distributed SNI controller \(T_c(s)\) with \(T_c(0) < 0\). Let \(r = 1_N \otimes r_0 \in \mathbb{R}^{3N}\) be the desired reference generated by the virtual leader agent, and \(d = [d_1, d_2, \ldots, d_N]^T \in \mathbb{R}^{3N}\) be the desired inter-aircraft spacing \((d_i \in \mathbb{R}^3 \forall i)\) along the \(X, Y\) and altitude coordinates. Then, the desired aircraft platooning objectives are fulfilled by the control scheme in Fig. 3, deploying the following distributed output feedback SNI control law

\[
U_i(s) = \beta T_c(s) \sum_{j \in \mathcal{N}_i} a_{ij} \left( (P_i(s) - d_i) - (P_j(s) - d_j) \right) + g_i(P_i(s) - d_i - r_0) \quad \forall i \in \{1, 2, \ldots, N\}
\]  

for any \(\beta \in (0, \infty)\). The notations \(U_i(s)\) and \(P_i(s)\) denote the Laplace Transform of the real-valued time-domain signals \(u_i(t)\) and \(p_i(t)\), respectively, for all \(t \geq 0\).

**Proof.** The closed-loop stability of the positive feedback interconnection of a distributed feedback-linearised aircraft agents \(I_N \otimes (I_3 \otimes \frac{1}{s^2})\) and a distributed SNI controller \((\mathcal{L} + \mathcal{G}) \otimes (I_3 \otimes \beta T_c(s))\) in Fig. 3 can be established by extending Theorem 1 for any \(\beta \in (0, \infty)\) under the condition \(T_c(0) < 0\). Let \(p = [p_1, p_2, \ldots, p_N]^T \in \mathbb{R}^{3N}\) denote the stacked position vector (i.e. the output vector) of all aircraft agents. We will now prove the asymptotic convergence of the tracking error, denoted as \(\xi = [\xi_1, \xi_2, \ldots, \xi_N]^T \in \mathbb{R}^{3N}\). The tracking error dynamics \(\dot{\xi}(s) = [I - ((\mathcal{L} + \mathcal{G}) \otimes (\beta \frac{1}{s^2} T_c(s) I_3))]^{-1} \ddot{R}(s)\) can be readily derived from Fig. 3. Then, the steady-state error \(\xi_{ss}\) can be obtained as follows:

\[
\dot{\xi}_{ss} = \lim_{t \to \infty} \dot{\xi}(t) = \lim_{s \to 0} s \ddot{R}(s) = \lim_{s \to 0} s[I - ((\mathcal{L} + \mathcal{G}) \otimes (\beta \frac{1}{s^2} T_c(s) I_3))]^{-1} \ddot{R}(s)
\]

[denote \(\ddot{R} = -(r + d)\) and \(\ddot{R}(s) = \text{Laplace of } \ddot{R}\)]

\[
\dot{\xi}_{ss} = \lim_{s \to 0} s^2[I - ((\mathcal{L} + \mathcal{G}) \otimes (\beta T_c(s) I_3))]^{-1} (s \ddot{R}(s)) = -[(\mathcal{L} + \mathcal{G}) \otimes (\beta T_c(0) I_3)]^{-1} (\lim_{s \to 0} s^2 I) \times \lim_{s \to 0} s \ddot{R}(s) = [0, 0, \ldots, 0]^T
\]

because \(T_c(0) < 0\), \((\mathcal{L} + \mathcal{G}) > 0\) and \(r(t)\) and \(d(t)\) are all bounded signals \(\forall t \geq 0\). Therefore, at the steady-state, \(p \to -\ddot{r} \to (r + d)\). Furthermore, this implies that the control objective in (5) holds when the desired inter-aircraft spacing is static, i.e., \(d\). However, for a time-varying but bounded formation configuration, i.e., \(d(t)\), the control objective in (6) remains valid. This completes the proof.

**Remark 1:** We assume the virtual leader agent is positioned at the front of the aircraft platoon, guiding all networked aircraft. By choosing a positive value for the projected distance in the altitude coordinate, i.e., \(d_h > 0\), the distributed output feedback SNI control law in (7) enables the networked aircraft to achieve the desired platoon during the descending and pre-landing phases. On the other hand, a negative value for the projected distance in the altitude coordinate, i.e., \(d_h < 0\), is selected for the taking-off phase.

**Remark 2:** When a runway fault occurs during the descending and pre-landing phases, the intelligent decision-making unit in Fig. 2b switches a descending aircraft platoon into a time-varying hover formation for each aircraft, ensuring a safe vertical gap is maintained.

**Algorithm 1** A distributed flight guidance and control system for aircraft platooning.

1. for each aircraft \(i \in \{1, 2, \ldots, N\}\) do
2. select an SNI controller \(T_c(s)\);
3. if Descending and Pre-landing then
4. choose \(d_h > 0\);
5. if A runway fault occurs then
6. choose a time-varying \(f_x(t)\) and \(f_y(t)\);
7. set a time-varying \(d_i(t)\);
8. compute the control protocol in (7);
9. else
10. set a static \(d_i\);
11. compute the control protocol in (7);
12. end if
13. else if Taking-off then
14. choose \(d_h < 0\);
15. set a static \(d_i\);
16. compute the control protocol in (7);
17. end if
18. end for
Building upon Theorem 2 and Remarks 1 and 2, we summarise the proposed distributed flight guidance and control system for aircraft platooning in Algorithm 1.

V. SIMULATION CASE STUDY

This section provides a MATLAB simulation case study to validate the effectiveness of the proposed NI theory-based two-loop aircraft platoon control scheme.

A. Regular aircraft landings

We considered a platoon of five aircraft agents and a virtual leader for a regular (or uninterrupted) aircraft landing scenario. All aircraft agents are connected through the interaction topology described in Fig. 4a. The primary objective is to ensure that the five networked aircraft agents maintain the desired inter-aircraft spacing by synchronising their velocities with a virtual leader agent. In the simulation, the virtual leader was given a forward velocity of 2 miles per minute and a descending velocity of \(-1000\) feet per minute. Each aircraft was required to maintain a projected distance of 3 miles in the \(X\) coordinate, 0 miles in the \(Y\) coordinate and 1000 feet in the altitude coordinate. An SNI controller \(T_c(s) = \frac{-3s^2+30s^2+90s+30}{s^2+15s^2+75s+125}\) was selected to be implemented as the outer loop controller in Fig. 2b.

Fig. 5 presents the results of the regular aircraft landing scenario. The aircraft flight trajectories in the \(X\) and altitude coordinates are illustrated in Fig. 5a. Furthermore, Fig. 5b shows the projected distances between successive aircraft, where each aircraft maintains the desired projected distances along the \(X\), \(Y\) and altitude coordinates. Fig. 5c indicates that the velocity of each aircraft achieves a constant speed synchronised with the virtual leader agent. These results validate that a group of five networked aircraft successfully achieved the objective of the regular aircraft landing. They effectively maintained the desired inter-aircraft spacing and synchronised their velocities with the virtual leader agent, employing the proposed aircraft platoon control scheme.

B. Aircraft landings in the event of a runway blockage

Next, we considered a scenario where a runway blockage occurs during aircraft landings. In such an event, the intelligent decision-making unit in Fig. 2b should switch a descending aircraft platoon into a time-varying hover formation for each aircraft at different altitudes while awaiting the resolution of the runway blockage. In this scenario, five aircraft, connected via the interaction topology described in Fig. 4b, were considered. Each aircraft was required to achieve a time-varying hover formation specified by

\[
\begin{bmatrix}
    d_{x,i}(t) \\
    d_{y,i}(t)
\end{bmatrix} = \begin{bmatrix}
    -3x + \cos(0.03t) \\
    0x + \sin(0.03t)
\end{bmatrix}
\forall i \in \{1, 2, ..., 5\}
\]

while maintaining a projected distance of 1000 feet in the altitude coordinate. An SNI controller \(T_c(s) = \frac{-3s^2+30s^2+90s+30}{s^2+15s^2+75s+125}\) was selected to be implemented as the outer loop controller in Fig. 2b.

Fig. 6 presents the results of the scenario where a runway blockage occurs during aircraft landings. The aircraft flight trajectories along \(X\), \(Y\) and altitude coordinates are illustrated in Fig. 6a, where each aircraft achieves a time-varying hover formation at a different altitude and maintains a constant vertical gap. Moreover, as shown in Fig. 6b, the 2-norm of the tracking error for each aircraft converges to zero. Fig. 6c shows the velocity of each aircraft across each coordinate. These results validate that five networked aircraft successfully transitioned to a time-varying hover formation during a runway blockage, employing the proposed aircraft platoon control scheme.

VI. CONCLUSIONS

This paper proposes a solution to air traffic management and control to accommodate the continuously increasing air traffic, particularly at busy airports, by introducing the idea of aircraft platooning. An NI theory-based two-loop aircraft platoon control scheme is developed to achieve the aircraft platooning objectives. The inner loop applies a feedback-linearising control action to transform the nonlinear translational dynamics of an aircraft into a three-input-three-output double-integrator system. While the outer loop implements a distributed output feedback SNI controller. In addition, a contingency strategy is devised that helps a descending aircraft platoon switch to a hover formation at different altitudes, maintaining a constant vertical gap while waiting for a clear landing runway. The simulation case study demonstrates the usefulness of the proposed NI theory-based aircraft platoon control scheme.

REFERENCES


Fig. 5. [Results for Case study 1:] (a) The aircraft flight trajectories in the X and altitude coordinates. The circles and triangles mark, respectively, the initial and final positions of the aircraft; (b) The projected distances between successive aircraft in the X, Y, and altitude coordinates; (c) The aircraft velocities in each coordinate. The units for $V_x$, $V_y$, and $V_h$ are miles/min, miles/min, and feet/min, respectively.

Fig. 6. [Results for Case study 2:] (a) The aircraft flight trajectories in the X, Y and altitude coordinates; (b) The 2-norm of the tracking error for each aircraft; (c) The aircraft velocities in each coordinate. The units for $V_x$, $V_y$, and $V_h$ are miles/min, miles/min, and feet/min, respectively.


